



# Firefly Algorithm Based Feature Selection for EEG Signal Classification

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**Abstract—** Brain-computer interfaces (BCIs) recognize specific features of a person's brain signal relating to his/her intent, and output a control command that controls the outside devices or computers. BCI systems facilitate the lives of patients who cannot move any muscles but have no cognitive disorder. The high dimensions of features represent a research challenge. In recent years, especially nature inspired heuristic optimization algorithms became popular in order to eliminate unnecessary features. This paper addresses a crucial factor for effective classification of motor imaginary based EEG signals that are an optimal selection of relevant EEG features using firefly algorithm. Firefly algorithm (FA) works on the principle of directing the less shiny than the light intensity emitted by fireflies in nature towards the bright. The algorithm can adaptively select the best subset of features and improve classification accuracy. In this study, following extracted Katz Fractal Dimension based features, effective feature(s) were selected by FA. The proposed method successfully applied on open access dataset which was collected from 29 subjects. We obtained an average 76.14% classification accuracy (CA) using  $k$ -nearest neighbor classifier. This is 4.4% higher than the CA calculated by using all features. These results proved that used method is robust for this dataset.

**Keywords—** electroencephalography; brain computer interface; katz fractal dimension; firefly algorithm;  $k$ -nearest neighbor

## I. INTRODUCTION

The main control center of the human body is the brain [1]. This control occurs when millions of nerve cells (neurons) that form the structural unit of the central nervous system communicate with each other. The electrical activity of the neurons forms the electroencephalography (EEG) signals, also known as the electrical picture of the brain [2]. EEG, which is recorded depending on electrical potential changes with electrodes placed in the skull, makes it possible to obtain and interpret the underlying information in the brain [3], [4]. Also, EEG signals form the basis of brain computer interface (BCI) systems [5]. In addition to use in different areas, BCI systems facilitate the lives of patients who cannot move any muscles but have no cognitive disorder. The basic BCI system commonly consists of pre-processing, feature extraction and classification steps. In recent years, studies have been focused on feature selection algorithms because reducing the dimensionality of features contributes to improve the

classification performance in BCI approaches [6]. It can also save storage and computation time and increase comprehensibility. Particularly, nature inspired heuristic optimization algorithms became popular [7]. In this study, we applied firefly algorithm (FA) to 2-class motor imaginary (MI) based EEG signals in order to enhance the performance of a classifier and obtain a rapid and high performance BCI system without redundant features.

In literature, there are a few feature selection methods to reduce feature dimension and BCI time [6]. However, most existing feature selection methods still suffer from stagnation in local optimal and/or high computational cost [8]. Thus, an efficient global search technique is needed to better solve feature selection problems. Genetic algorithm (GA) [9], artificial bee colony [10], particle swarm optimization [11] are some of the feature selection algorithms that have been recently used in BCI studies. Hsu et al. (2010) proposed a method using subband nonlinear parameters and GA for automatic seizure detection in EEG. They used discrete wavelet transform as feature extracted method and employed as the features to train the support vector machine (SVM) with linear kernel function and radial basis function kernel function classifiers. Then, the GA was used for selecting the effective feature subset. However, the disadvantage of GA takes a long time to converge to the optimal solution [12]. In another feature selection based study, Rakshit et al. (2012) worked with MI based EEG signals. In their paper, they aimed to eliminate the redundant features of a dataset to improve the accuracy of classification. To do so, they employed artificial bee colony cluster algorithm to reduce the feature dimension. They calculated the highest classification accuracy (CA) as 64.29%. However, local search ability of this algorithm was weak [13].

In this paper, we used FA based feature selection method to select effective features because the parameters that need to be controlled are relatively few, and the precision optimization and convergence speed are high [14] compared to other algorithms. Firstly, we applied fourth order of Chebyshev type II filter (passband of 0.5 - 50 Hz) to the EEG data using the Berlin BCI toolbox [15]. Secondly, after Katz Fractal Dimension (KFD) was used for extracting features from signals, an FA algorithm based optimizing feature selection

method was employed to identify the effective classification feature(s). Finally, we achieved average 76.14% CA from 29 subjects using  $k$ -nearest neighbor ( $k$ -NN) classifier. This result is 4.4% higher than the CA calculated using all feature(s). The results proved that the proposed method is successful for this dataset.

## II. MATERIAL AND METHOD

### A. Dataset Description

Open access dataset [16] was recorded in an ordinary bright room from 29 subjects. The experimental procedure consists of three sections which is given in Figure 1. Each section has a resting period of 60 seconds (sec) before the experiment. After 2 sec visual presentation was exhibited in the middle of the screen, task period was performed for 10 sec. During the 10 sec, subjects were asked to imagine right/left hand opening-closing. Then after a 1 sec "STOP" warning, rest period was performed with a 15-17 sec. Finally, a single section was terminated with a 60 sec post-rest.

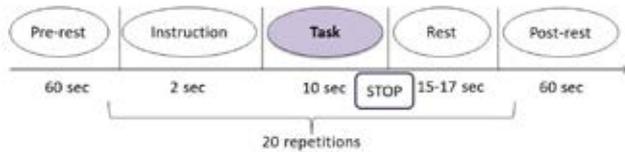


Figure 1. Experimental procedure [16]

20 trials were recorded in each section. A total of 60 trials were recorded in three sections. 30 trials are labeled as *class 0* (right hand opening-closing) while rest of them are labeled as *class 1* (left hand opening-closing). This dataset is sampled at 200 Hz and each trial consists of 2000 samples for a task period. Also, this dataset was recorded with thirty electrodes (1. AFp1, 2. AFp2, 3. AFF1h, 4. AFF2h, 5. AFF5h, 6. AFF6h, 7. F3, 8. F4, 9. F7, 10. F8, 11. FCC3h, 12. FCC4h, 13. FCC5h, 14. FCC6h, 15. T7, 16 T8, 17. Cz, 18. CCP3h, 19. CCP4h, 20. CCP5h, 21. CCP6h, 22. Pz, 23. P3, 24. P4, 25. P7, 26. P8, 27. PPO1h, 28. PPO2h, 29. POO1, 30. POO2 and Fz for ground electrode) which were placed as given in Figure 2.

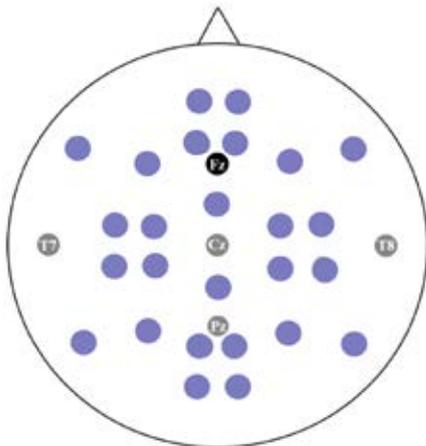


Figure 2. Electrode positions for dataset [16]

### B. Proposed Method

The application procedure of the proposed method is given in Figure 3. Firstly, pre-processed EEG trials are separated by 50% randomly as training and test set. Then, KFD based feature(s) were extracted from each of these sets. During the training stage, effective feature(s) were selected with FA algorithm and the robust feature(s) in the test set were classified. Finally, the CA, sensitivity (SE), specificity (SP) and kappa coefficient ( $\kappa$ ) were calculated for evaluating the performance of the  $k$ -NN.

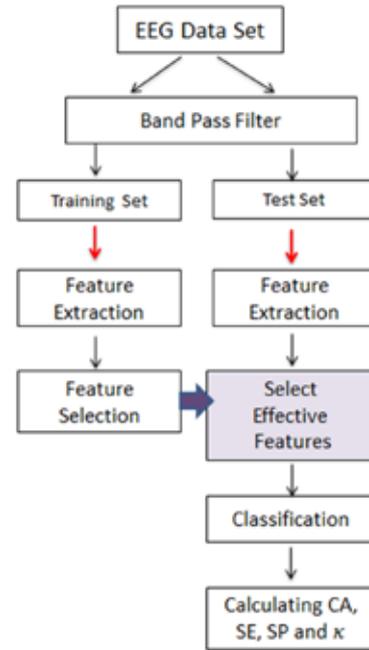


Figure 3. Flow chart of NIRS data analysis

#### 1) Katz Fractal Dimension

We used Katz fractal dimension for extracting features. In the Katz's algorithm, Katz [17] the FD is obtained directly from the time series.  $P$  is the sum of the distance between successive data points in the signal  $Y$  ( $[x_1 y_1; x_2 y_2; \dots; x_n y_n]$ ) is given in Equation 1. In this equation,  $n$  represents the size of  $Y$ .

$$P = \sum_{n=1}^{n-1} \sqrt{(x_n - x_{n+1})^2 + (y_n - y_{n+1})^2} \quad (1)$$

The  $H$ , given in Equation 2, is the distance between the first point in the  $Y$  and the point at the farthest distance from the first point.

$$H = \max[\sum_{n=1}^n \sqrt{(x_1 - x_n)^2 + (y_1 - y_n)^2}] \quad (2)$$

The Katz fractal dimension of the waveform is defined as in Equation 3 depending on  $P$  and  $H$  [18]. In this equation,  $z$  is the number of steps in the waveform.

$$FD = \frac{\log(z)}{\log(H/P) + \log(z)} \quad (3)$$

### 2) Feature Selection

In this study, firefly algorithm was used for feature(s) selection. This algorithm is herd-based Heuristic Optimization Algorithm which developed by Xin-She Yang in 2008 [19]. It was developed by considering the brightness-sensitive social behavior of fireflies. Algorithm operation consists of the following steps;

- Random positions of fireflies are determined. Then the brightness is calculated.
- Fireflies move towards more bright fireflies.
- Return to stage (b) until the specified number of iterations is reached.

Brightness between  $x^{th}$  and  $y^{th}$  fireflies varies with respect to the distance and brightness decreases as the distance increases. A firefly's brightness which is seen by another firefly, is calculated as in Equation 4.

$$B(a) = B_0 e^{-\gamma a} \quad (4)$$

where  $B_0$  is the brightness at  $a = 0$  ( $a$  is the distance between any two fireflies),  $\gamma$  is a light absorption coefficient which controls the decrease in light intensity.  $x^{th}$  firefly is attracted by  $y^{th}$  firefly, and the movement is given in Equation 5.

$$m_x^{in+1} = B_0 e^{-\gamma(r_{xy})^2} (m_y^{in} - m_x^{in}) + \beta(RN - 0.5) \quad (5)$$

where  $in$ ,  $\beta$  and  $RN$  mean iteration number, randomization parameter and random number generator, respectively.  $RN$  uniformly generates numbers between 0 and 1. Also,  $r_{xy}$  is the distance between the  $x^{th}$  firefly and the  $y^{th}$  firefly, which is defined by the Equation 6. In this equation,  $T$  ( $i = 1 \dots T$ ) is the number of dimensions. In this study,  $T$  is 30 indicating the total number of features calculated by *KFD*.

$$r_{xy} = \|m_x - m_y\| = \sqrt{\sum_{i=1}^T (m_{xi} - m_{yi})^2} \quad (6)$$

Each firefly is moving in a direction in the searching space to find the effective feature(s) based on the accuracy of the classifier model with the selected effective features [14].

### 3) Classification

The  $k$ -NN algorithm stores all current states and classifies new states according to a similarity measure. This method classifies data based on similarity measure by examining the  $k$  closest neighboring distances [20]. In this study, we tested cosine as the distance measurement as given in Equation 7.

$$\cos(\theta) = \frac{f \cdot g}{\|f\| \|g\|} = \frac{\sum_{i=1}^T f_T(X_i) g_T(Y_i)}{\sqrt{\sum_{i=1}^T f_T(X_i)^2} \sqrt{\sum_{i=1}^T g_T(Y_i)^2}} \quad (7)$$

where  $T$  represents the number of features. Additionally,  $f_T(X_i)$  and  $g_T(Y_i)$  state the value of  $T^{th}$  feature of  $X_i$  and the value of  $T^{th}$  feature of  $Y_i$ , respectively. Also,  $X_i$  and  $Y_i$  are the components of vector  $X$  and  $Y$ , respectively. It is worthwhile mentioning that in this study, we calculated SE and SP values as correct classification percentage of the class 0 and class 1. Furthermore, the optimum  $k$  parameter was decided by random sub-sampling method.

## III. RESULTS AND DISCUSSION

In this study, *KFD* based features were extracted from the *MI* based EEG signals which were recorded from 29 subjects. Then, effective feature(s) were selected using by *FA*. These selected feature(s) were classified with  $k$ -NN for 100-times run using the cross validation method. *CA*, *SE* and *SP* values calculated for 29 people with the selected effective features are given as radar plot in Figure 4. In Figure 4, we achieved an average 76.14% *CA*, 76.52% *SE* and 75.77% *SP*, respectively.

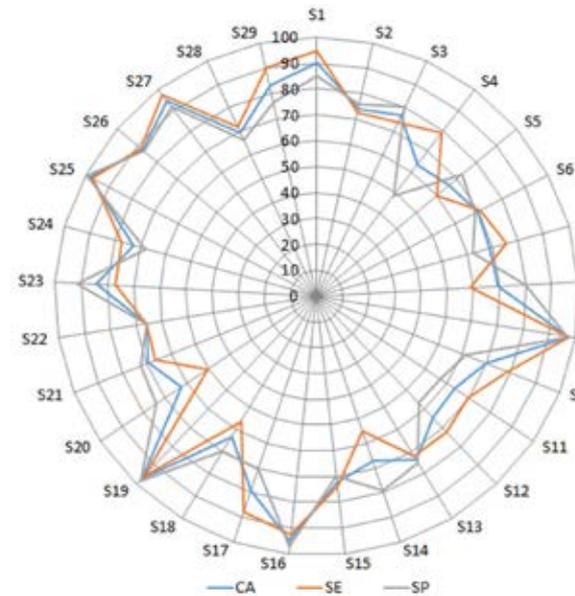


Figure 4. CAs, SEs and SPs calculated with *FA*

To show the effectiveness of the proposed method, we also obtained classification results using all features. In Figure 5, we showed the classification results of 29 subjects with radar plots in terms of *CAs*, *SEs* and *SPs*. Their average values were calculated as 71.74, 72.05% and 71.43% respectively. In these radar graphs, all subjects from 1 to 29 are expressed as  $S_1, S_2, S_3, \dots, S_{29}$ , respectively.

Moreover, we calculated kappa coefficients as given in Figure 6 and 7 for 29 subjects with cross-validation analysis over 100-times run on the with *FA* (with selected effective feature(s)) and all feature. According to these values, average 0.52 and 0.43 kappa coefficients were achieved.

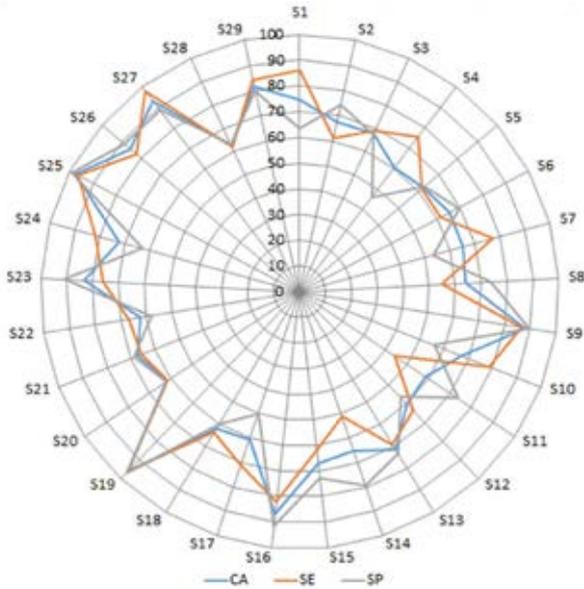


Figure 5. CAs, SEs and SPs calculated with all features

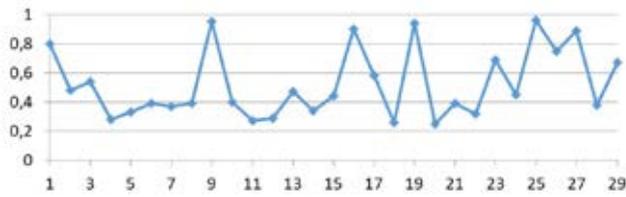


Figure 6. Kappa coefficients with FA calculated from 29 subjects

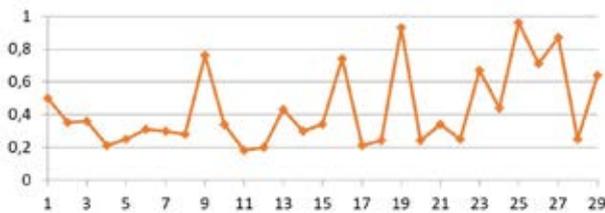


Figure 7. Kappa coefficients with all features calculated from 29 subjects

We used a FA for feature selection to choose minimal number of features and to obtain even better classification accuracy by utilizing all features. The achieved results verified that FA is an effective search algorithm for feature selection problems. Further, effective feature(s) selected by FA can enhance the performance of right/left hand opening-closing motor imagery BCI application.

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